



Enzymes

Part III: Enzyme kinetics

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Kinetics



- Kinetics is deals with the rates of chemical reactions.
- Chemical kinetics is the study of the rates of chemical reactions.
- For the reaction ($A \rightarrow P$), The velocity, v , or rate, of the reaction is the amount of P formed or the amount of A consumed per unit time, t . That is,

$$v = \frac{d[P]}{dt}$$

or

$$v = \frac{-d[A]}{dt}$$

Rate law



- The mathematical relationship between reaction rate and concentration of reactant(s) is the rate law (*the mathematical equation describing how the concentrations of reactants affect the rate of the reaction during a certain period*).
- For the reaction ($A \rightarrow P$), the rate law is

$$v = \frac{-d[A]}{dt} = k[A]$$

- From this expression, the rate is proportional to the concentration of A, and k is the rate constant.
 - k has the units of $(\text{time})^{-1}$, usually sec^{-1} .

First-order reaction

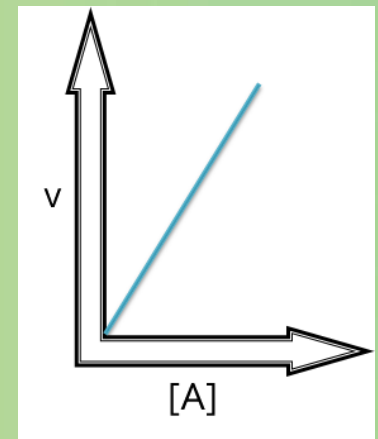
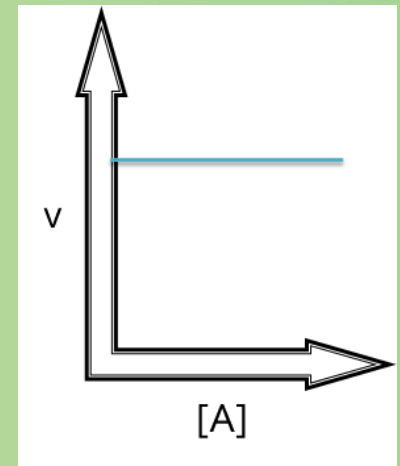


- Since reaction order refers to the number of molecules involved in a reaction, the simple reaction of $A \rightarrow P$ is a first-order reaction.
- The rate of the reaction is directly proportional to the concentration of the reactant.
- Thus, as the concentration of A is reduced, the rate of the reaction slows down, and vice versa.

Zero- vs. first-order reaction



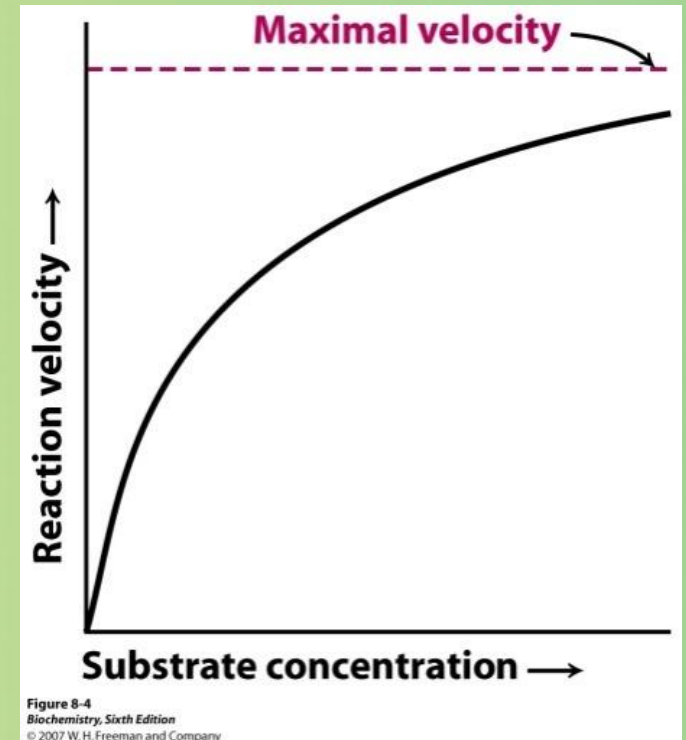
Overall order	$V =$	Dimensions of k
Zero	k	$(\text{conc.})(\text{time})^{-1}$
First	$k[A]$	$(\text{time})^{-1}$



Enzyme kinetics



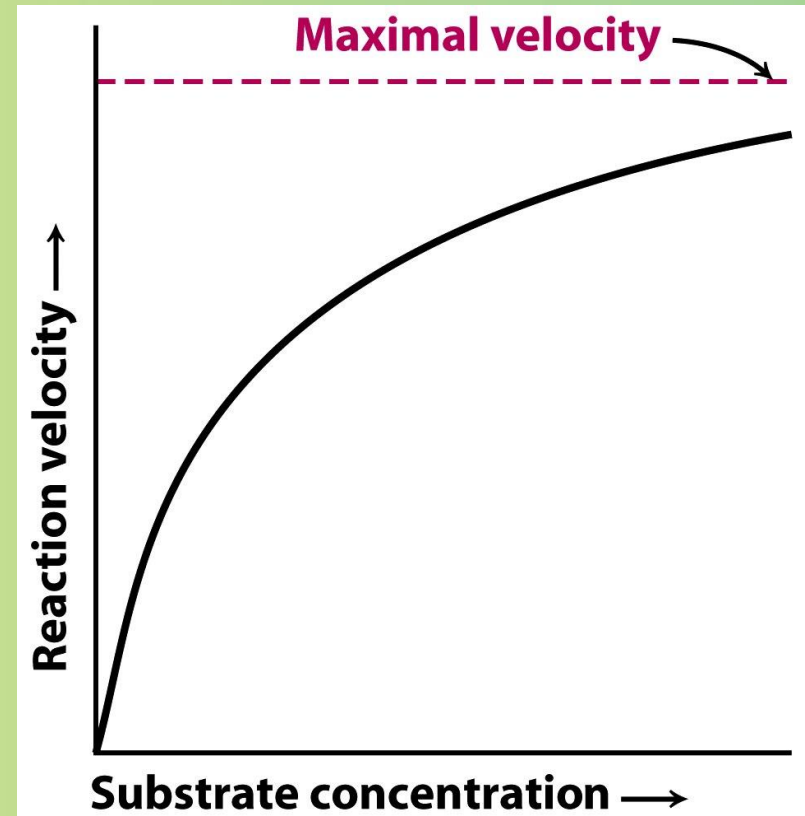
- The kinetics of the enzyme-catalyzed reactions are different than those of a typical chemical reaction,
 - Enzyme-catalyzed reactions have hyperbolic plots.
- The study of enzyme kinetics addresses the biological roles of enzymatic catalysts.



How?



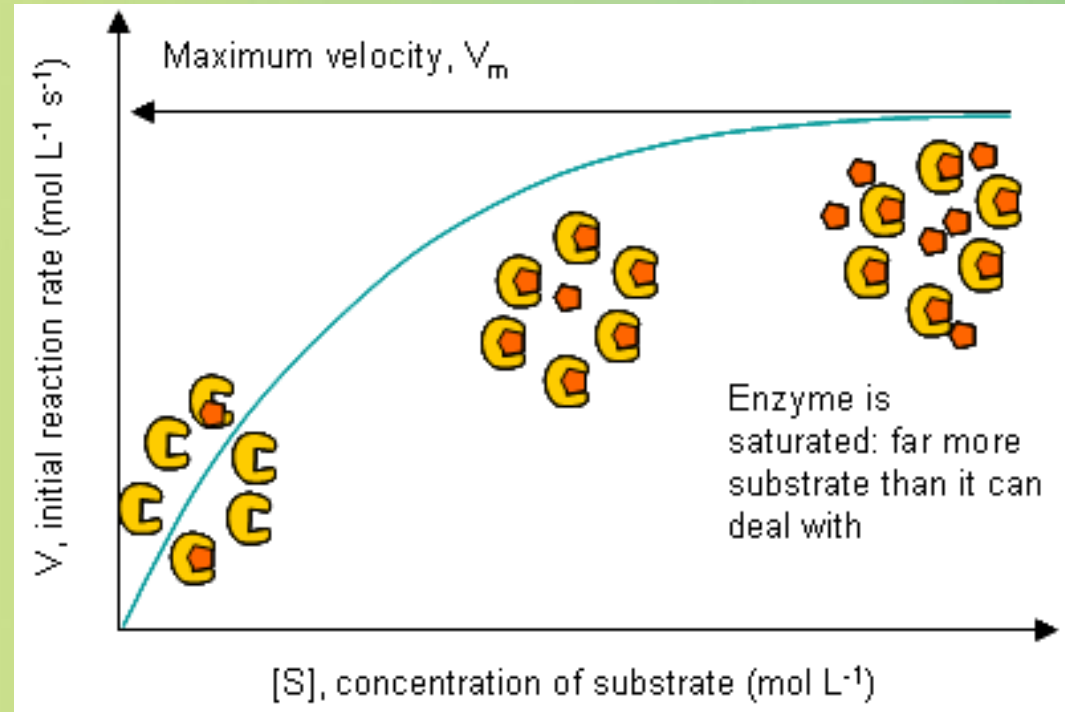
- For many enzymes, initial velocity (V_0) varies with the substrate concentration $[S]$.
- The rate of catalysis rises linearly as substrate concentration increases and then begins to level off and approach a maximum at higher substrate concentrations.



Why?



- The hyperbolic plot is known as a saturation plot because the enzyme becomes "saturated" with substrate, i.e. each enzyme molecule has a substrate molecule associated with it.



More explanation

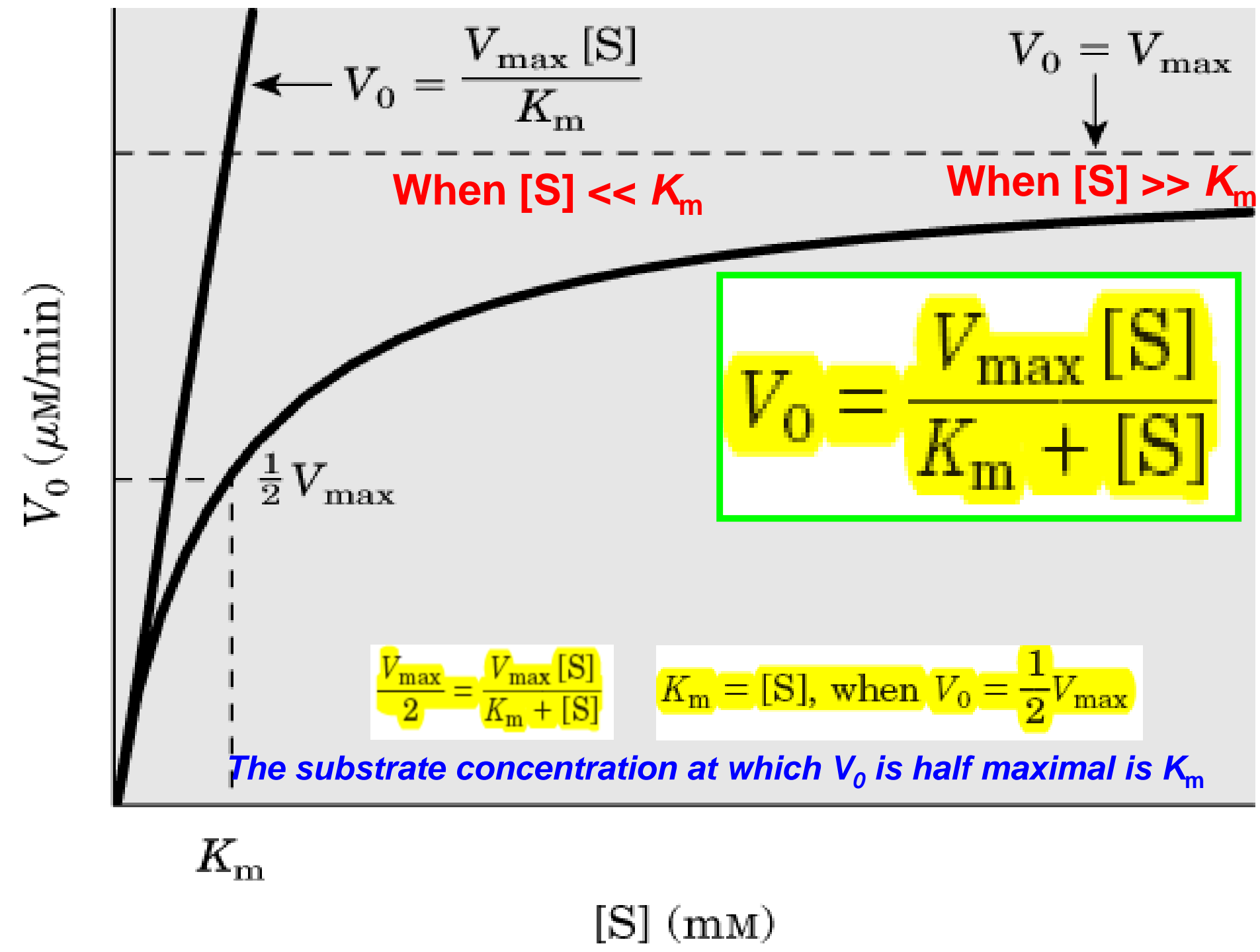


- At a fixed concentration of enzyme, V_0 is almost linearly proportional to $[S]$ when $[S]$ is small.
- However, V_0 is nearly independent of $[S]$ when $[S]$ is large
- The maximal rate, V_{max} , is achieved when the catalytic sites on the enzyme are saturated with substrate.
- V_{max} reveals the turnover number of an enzyme.
 - The number of substrate molecules converted into product by an enzyme molecule in a unit time when the enzyme is fully saturated with substrate.
- At V_{max} , the reaction is in zero-order rate since the substrate has no influence on the rate of the reaction.

The Michaelis-Menten equation

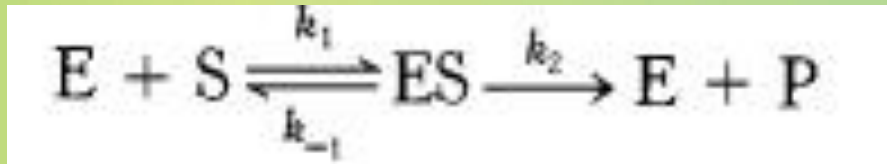
- Two scientists, Leonor Michaelis and Maud Menten, proposed a simple model to describe enzyme kinetics.
- The Michaelis-Menten equation is a quantitative description of the relationship between the rate of an enzyme catalyzed reaction (V_0), substrate concentration $[S]$, a rate constant (K_M) and maximal velocity (V_{max}).

$$V_0 = V_{max} \frac{[S]}{[S] + K_M}$$



The Michaelis constant (K_m)

- For a reaction:



- K_M , called the Michaelis constant is

$$K_M = \frac{k_{-1} + k_2}{k_1}$$

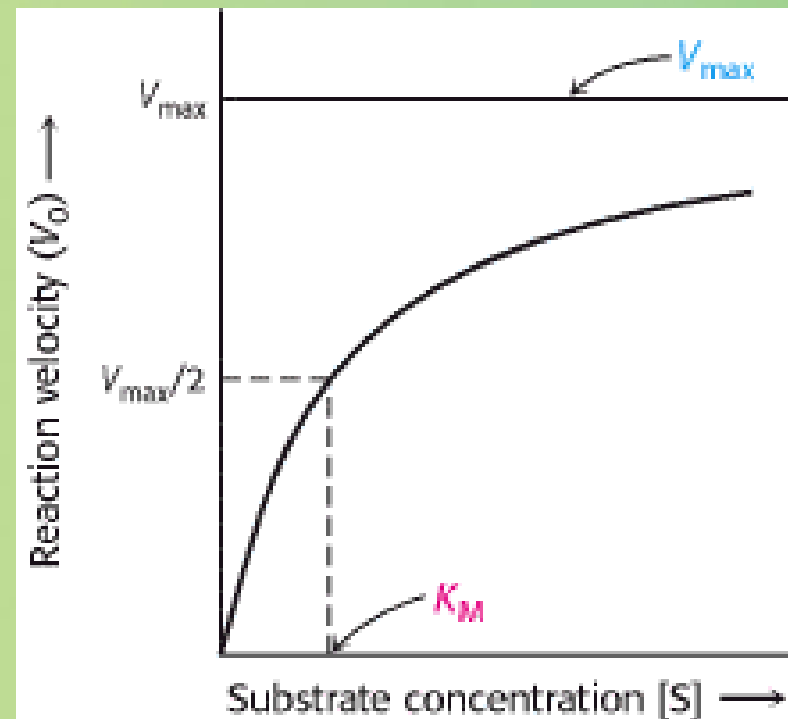
- In other words, K_m is related to the rate of dissociation of substrate from the enzyme to the enzyme-substrate complex
- K_m describes the affinity of enzyme for the substrate.

K_m



- K_M is the concentration of substrate at which half the active sites are filled.
- When $[S] = K_M$, then $V_0 = V_{max}/2$
- Therefore, it provides a measure of enzyme affinity towards a substrate.
- The lower the K_M of an enzyme towards a substrate is, the higher its affinity to the same substrate is.

$$V_0 = V_{max} \frac{[S]}{[S] + K_M}$$



$$V_0 = V_{\max} \frac{[S]}{[S] + K_M}$$

- At very low substrate concentration, when $[S]$ is much less than K_M , $V_0 = (K_M)[S]$; that is, the rate is directly proportional to the substrate concentration.
- At high substrate concentration, when $[S]$ is much greater than K_M , $V_0 = V_{\max}$; that is, the rate is maximal, independent of substrate concentration.

Note



- Each substrate will generate a unique K_M and V_{max} for a given enzymatic process.
- The K_M values of enzymes range widely.
- For most enzymes, K_M lies between 10^{-1} and 10^{-7} M.

table 8-6

K_m for Some Enzymes and Substrates

Enzyme	Substrate	K_m (mM)
Catalase	H_2O_2	25
Hexokinase (brain)	ATP	0.4
	D-Glucose	0.05
	D-Fructose	1.5
Carbonic anhydrase	HCO_3^-	26
Chymotrypsin	Glycyltyrosinylglycine	108
	N-Benzoyltyrosinamide	2.5
β -Galactosidase	D-Lactose	4.0
Threonine dehydratase	L-Threonine	5.0

Example



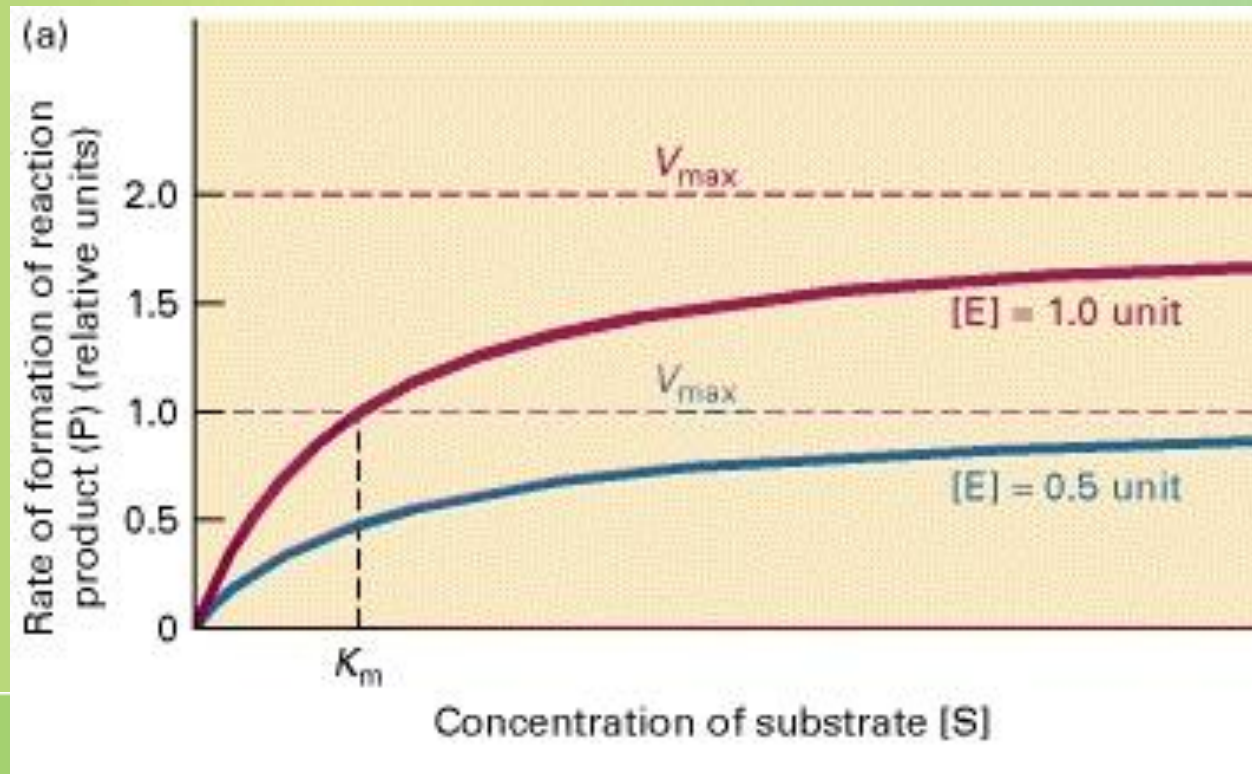
- A biochemist obtains the following set of data for an enzyme that is known to follow Michaelis-Menten kinetics. Approximately, V_{max} of this enzyme is ... & K_M is ...?

- 5000 & 699
- 699 & 5000
- 621 & 50
- 94 & 1
- 700 & 8

Substrate Concentration (μM)	Initial velocity ($\mu\text{mol/min}$)
1	49
2	96
8	349
50	621
100	676
1000	698
5000	699

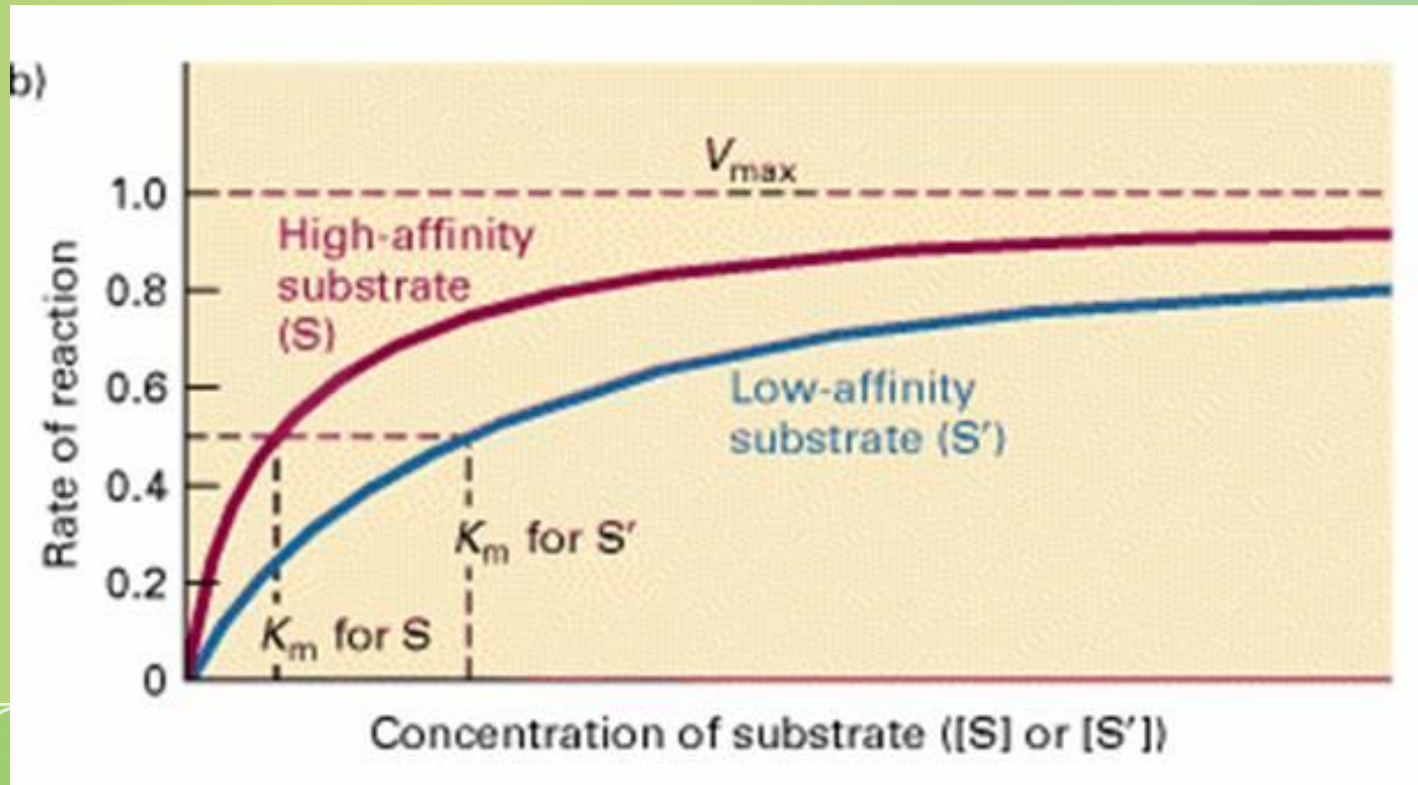
Example 1 of K_M

- Doubling the concentration of enzyme causes a proportional increase in the reaction rate, so that the maximal velocity V_{max} is doubled; the K_M , however, is unaltered



Example 2 of K_M

- A reaction is catalyzed by an enzyme with substrate S (high affinity) and with substrate S' (low affinity).
- V_{max} is the same with both substrates, but K_M is higher for S', the low-affinity substrate.





Biological significance of Km

Effect of alcohol



- The physiological consequence of K_M is illustrated by the sensitivity of some individuals to ethanol.
- Such persons exhibit facial flushing and rapid heart rate (tachycardia) after ingesting even small amounts of alcohol.



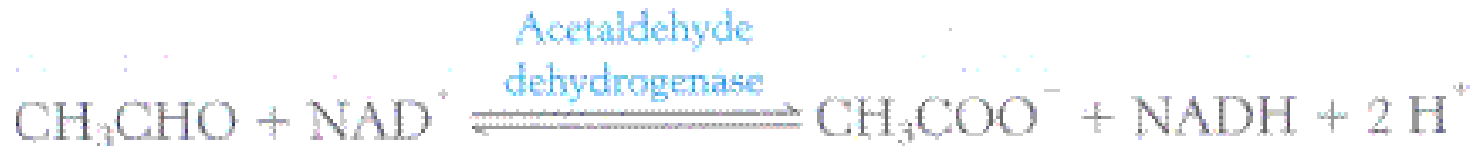
Enzymatic reactions



- In the liver, alcohol dehydrogenase converts ethanol into acetaldehyde.



- Normally, the acetaldehyde, which is the cause of the symptoms when present at high concentrations, is processed to acetate by acetaldehyde dehydrogenase.



The effect



- Most people have two forms of the acetaldehyde dehydrogenase, a low K_M mitochondrial form and a high K_M cytosolic form.
 - These are called isozymes (keep that in mind)
- In vulnerable persons, the mitochondrial enzyme is less active due to the substitution of a single amino acid, and acetaldehyde is processed only by the cytosolic enzyme.
- Because the cytosolic enzyme has a high K_M , less acetaldehyde is converted into acetate; excess acetaldehyde escapes into the blood and causes the physiological effects.

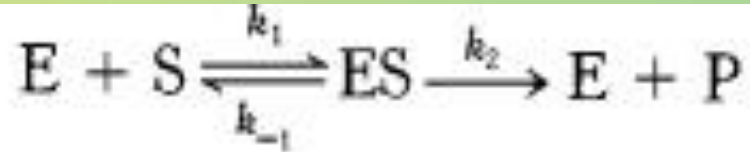


Measurements of enzyme kinetics

V_{max} & k_{cat}



➤ For the enzymatic reaction



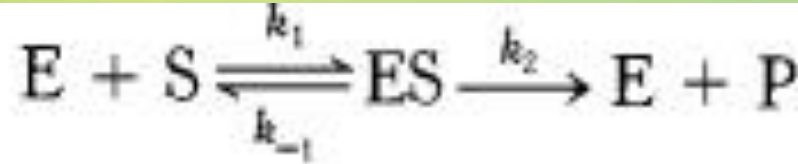
➤ The maximal rate, V_{\max} , is equal to the product of k_2 , also known as k_{cat} , and the total concentration of enzyme.

$$V_{\max} = k_2 [E]_T$$

Turnover Numbers (k_{cat}) of Some Enzymes

Enzyme	Substrate	k_{cat} (s ⁻¹)
Catalase	H ₂ O ₂	40,000,000
Carbonic anhydrase	HCO ₃ ⁻	400,000
Acetylcholinesterase	Acetylcholine	14,000
β-Lactamase	Benzylpenicillin	2,000
Fumarase	Fumarate	800
RecA protein (an ATPase)	ATP	0.4

Kcat



- **k_{cat}**, the turnover number, is the concentration (or moles) of substrate molecules converted into product per unit time per concentration (or moles) of enzyme, or when fully saturated.
- It describes how quickly an enzyme acts, i.e. how fast the ES complex proceeds to E + P.
- In other words, the maximal rate, V_{max}, reveals the turnover number of an enzyme if the total concentration of active sites [E]_T is known.
- **k_{cat}** is a constant you can look up for any given enzyme.

$$k_{\text{cat}} = V_{\text{max}} / [E]_{\text{T}}$$

Example



- You are working on the enzyme “Medicine” which has a molecular weight of 50,000 g/mol. You have used 10 μg of the enzyme in an experiment and the results show that the enzyme at best converts 9.6 μmol of the substrate per min at 25°C. The turnover number (kcat) for the enzyme is:

A. 9.6 s^{-1}

B. 48 s^{-1}

C. 800 s^{-1}

D. 960 s^{-1}

E. 1920 s^{-1}

Example



- a 10^{-6} M solution of carbonic anhydrase catalyzes the formation of 0.6 M H_2CO_3 per second when it is fully saturated with substrate.
 - ✓ Hence, k_{cat} is $6 \times 10^5 \text{ s}^{-1}$
 - ✓ 10^4 min^{-1}
- Each catalyzed reaction takes place in a time equal to $1/k_2$, which is $1.7 \mu\text{s}$ for carbonic anhydrase.
- The turnover numbers of most enzymes with their physiological substrates fall in the range from 1 to 10^4 per second.

40,000,000 molecules of H_2O_2 are converted to H_2O and O_2 by ONE catalase molecule within one second



table 8-7

Turnover Numbers (k_{cat}) of Some Enzymes

Enzyme	Substrate	k_{cat} (s^{-1})
Catalase	H_2O_2	40,000,000
Carbonic anhydrase	HCO_3^-	400,000
Acetylcholinesterase	Acetylcholine	14,000
β -Lactamase	Benzylpenicillin	2,000
Fumarase	Fumarate	800
RecA protein (an ATPase)	ATP	0.4

Kcat vs. Km



Table 6.2

Turnover Numbers and Km for Some Typical Enzymes

Enzyme	Function	k_{cat} = Turnover Number*	K_M **
Catalase	Conversion of H_2O_2 to H_2O and O_2	4×10^7	25
Carbonic Anhydrase	Hydration of CO_2	1×10^6	12
Acetylcholinesterase	Regenerates acetylcholine, an important substance in transmission of nerve impulses, from acetate and choline	1.4×10^4	9.5×10^{-2}
Chymotrypsin	Proteolytic enzyme	1.9×10^2	6.6×10^{-1}
Lysozyme	Degrades bacterial cell-wall polysaccharides	0.5	6×10^{-3}

k_{cat} values vary over a range of nearly 2×10^7

K_M values vary over a range of nearly 4000

k_{cat}/K_M , the range is near 10^3

Specificity & Efficiency: Physiological $[S]/K_M$



- Most enzymes are not normally fully saturated.
- Under physiological conditions, the $[S]/K_M$ ratio is typically between 0.01 and 1.0
- Specificity constant (k_{cat}/K_M): is also called catalytic efficiency tells us how rapidly the enzyme binds and how quickly it turns over.
- k_{cat}/K_M ($\text{M}^{-1} \text{min}^{-1}$) is indicative of:
 - ✓ Enzyme's substrate specificity: the higher the ratio, the higher the specificity.
 - ✓ Enzyme's catalytic efficiency: the higher the ratio, the more efficient the enzyme.

$$V = \frac{V_{\text{max}} [S]}{K_M + [S]} = \frac{k_{\text{cat}} [E_T][S]}{K_M + [S]}$$

$$V = (k_{\text{cat}}/K_M) [E][S]$$

Rate of reaction (velocity)



- Rate of reaction is calculated as concentration of substrate disappearing (or concentration of product appearing) per unit time ($\text{mol L}^{-1} \cdot \text{sec}^{-1}$ or $\text{M} \cdot \text{sec}^{-1}$).

Enzyme activity



- In order to measure enzyme activity, we measure the number of moles of substrate disappearing (or products appearing) per unit time ($\text{mol} \cdot \text{sec}^{-1}$)
- In other words,
enzyme activity = rate of reaction \times reaction volume

Specific activity



- Specific activity is a measure of enzyme purity and quality.
- It is calculated as moles of substrate converted per unit time per unit mass of enzyme ($\text{mol} \cdot \text{sec}^{-1} \cdot \text{g}^{-1}$).
- In other words,

Specific activity = enzyme activity / mass of enzyme (grams)

- This is useful in determining enzyme purity after purification.

Turnover number



- Turnover number (k_{cat}) is related to the specific activity of the enzyme where it is

Turnover number = specific activity \times molecular weight of enzyme

- It is expressed as moles of substrate converted per unit time (usually per second)/moles of enzyme (min^{-1} or sec^{-1})
- Remember: $k_{cat} = V_{max} / [E]_T$

Sample calculations:

A solution contains initially $25.0 \times 10^{-4} \text{ mol L}^{-1}$ of peptide substrate and $1.50 \mu\text{g}$ chymotrypsin, in 2.5 mL volume. After 10 minutes, $18.6 \times 10^{-4} \text{ mol L}^{-1}$ of peptide substrate remain. Molar mass of chymotrypsin is $25,000 \text{ g mol}^{-1}$.

peptide substrate consumed $= 6.4 \times 10^{-4} \text{ mol L}^{-1}$ in 10 minutes

Rate of reaction $= 6.4 \times 10^{-5} \text{ mol L}^{-1} \text{ min}^{-1}$

Enzyme activity
(rate \times volume) $= 6.4 \times 10^{-5} \text{ mol L}^{-1} \text{ min}^{-1} \times 2.5 \times 10^{-3} \text{ L}$
 $= 1.6 \times 10^{-7} \text{ mol min}^{-1}$

Specific activity
(activity / mass) $= 1.6 \times 10^{-7} \text{ mol min}^{-1} / 1.50 \mu\text{g}$
 $= 1.1 \times 10^{-7} \text{ mol } \mu\text{g}^{-1} \text{ min}^{-1}$

Turnover number
(sp. act. \times molar mass) $= 1.1 \times 10^{-7} \text{ mol } \mu\text{g}^{-1} \text{ min}^{-1} \times 25,000 \text{ g mol}^{-1} \times 10^6 \mu\text{g g}^{-1}$
 $= 2.7 \times 10^3 \text{ min}^{-1} = 45 \text{ s}^{-1}$

Disadvantage of Michaelis-Menten equation

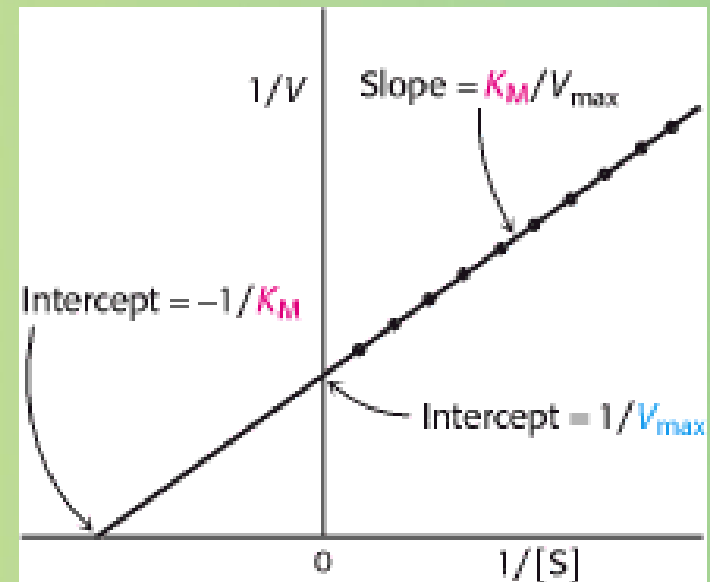


- Determination of K_m from hyperbolic plots is not accurate since a large amount of substrate is required in order to reach V_{max} .
- This prevents the calculation of both V_{max} and K_M .

The Lineweaver-Burk or double-reciprocal plot



- A plot of $1/V_0$ versus $1/[S]$, called a Lineweaver-Burk or double-reciprocal plot, yields a straight line with an intercept of $1/V_{max}$ and a slope of K_M/V_{max} .
- The intercept on the x-axis is $-1/K_M$.

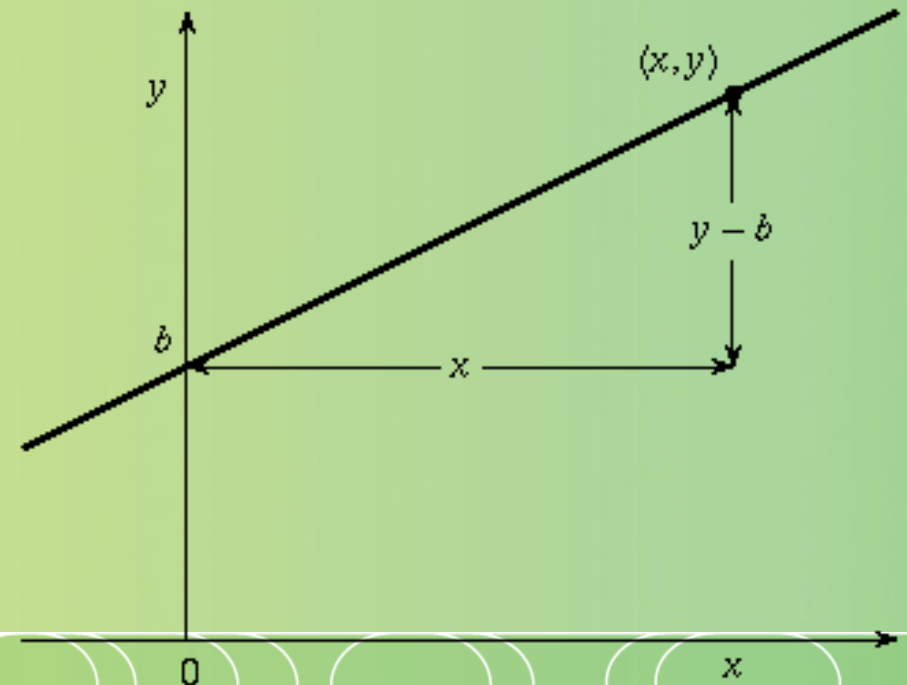


$$\frac{1}{V_0} = \frac{1}{V_{max}} + \frac{K_M}{V_{max}} \cdot \frac{1}{[S]}$$

$$\frac{1}{V_0} = \frac{1}{V_{\max}} + \frac{K_M}{V_{\max}} \cdot \frac{1}{[S]}$$

$$y = b + mx$$

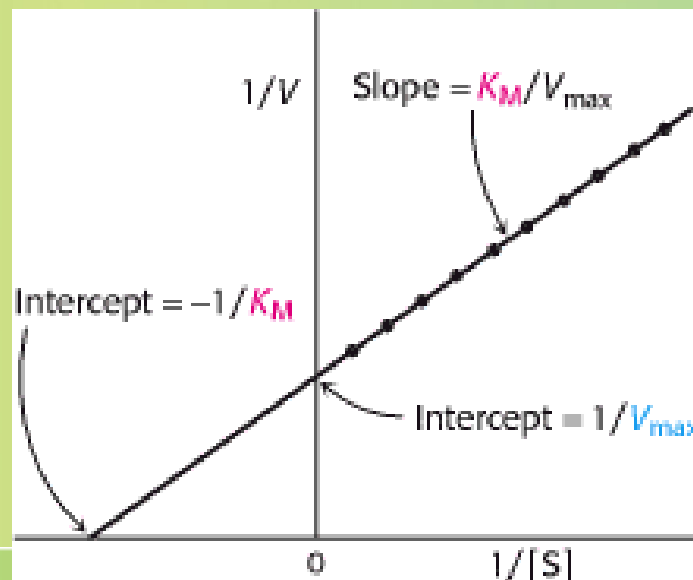
- y is y-axis = $1/V_0$
- x is x-axis = $1/[S]$
- m is slope = K_M/V_{\max}
- B is $1/V_{\max}$



$$\frac{1}{V_0} = \frac{1}{V_{\max}} + \frac{K_M}{V_{\max}} \cdot \frac{1}{[S]}$$

$$y = b + mx$$

- If $x = 0$, then $y = b$ (x-axis is 0, then y-intercept = $1/V_{\max}$)



$$\frac{1}{V_0} = \frac{1}{V_{\max}} + \frac{K_M}{V_{\max}} \cdot \frac{1}{[S]}$$

$$y = b + mx$$

If $y = 0$, then $mx = -b$ (y-axis is 0, then x-intercept = $-1/K_M$)

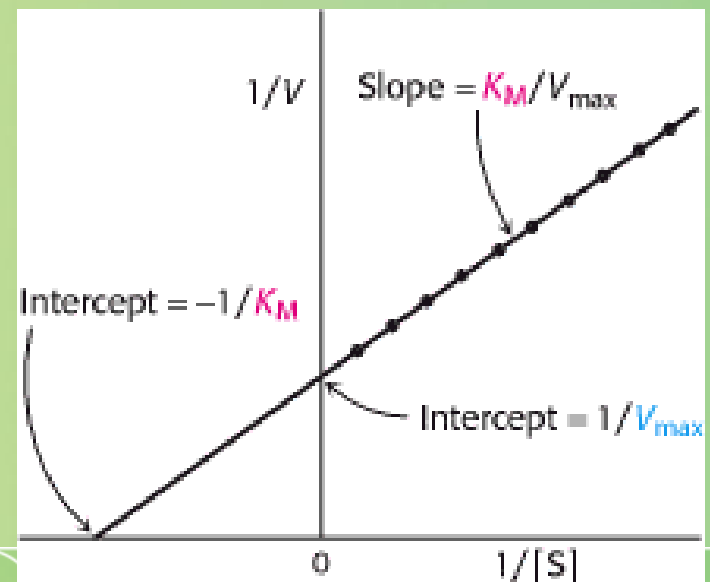
How?

$$0 = 1/V_{\max} + (K_M/V_{\max}) \cdot (1/[S])$$

$$-1/V_{\max} = (K_M/V_{\max}) \cdot (1/[S])$$

$$-1 = K_M \cdot (1/[S])$$

$$-1/K_M = 1/[S]$$



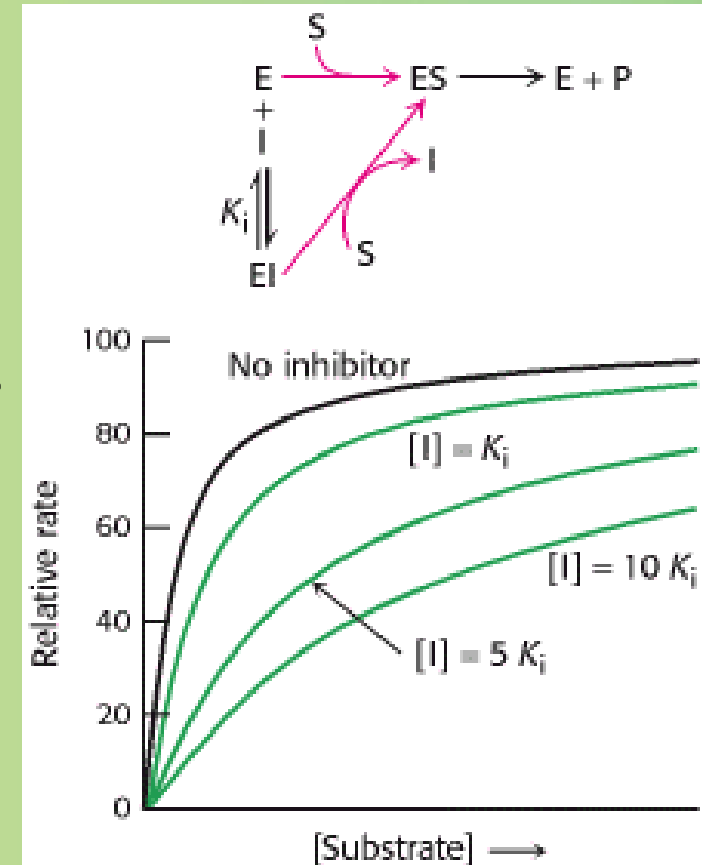
Enzyme inhibitors



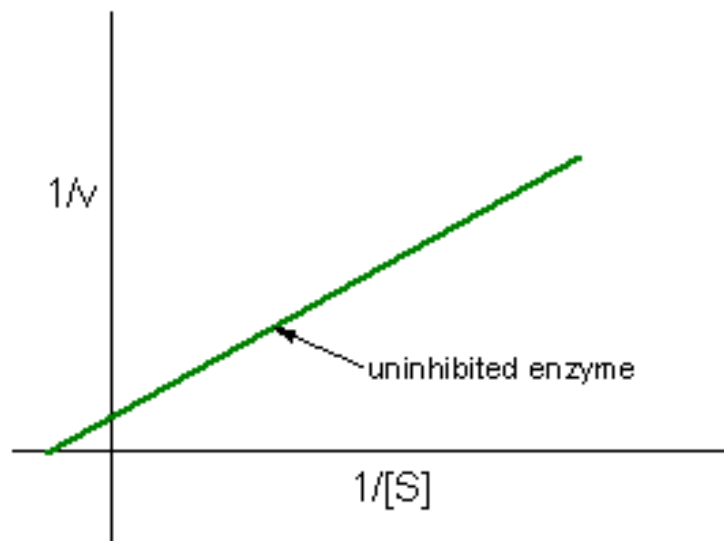
- Enzyme inhibition can be either reversible or irreversible.
- An irreversible inhibitor dissociates very slowly from its target enzyme because it has become tightly bound to the enzyme, mainly covalently.
 - The kinetic effect of irreversible inhibitors is to decrease the concentration of active enzyme.
- Reversible inhibition is characterized by a rapid dissociation of the enzyme-inhibitor complex.
 - Usually these inhibitors bind to enzymes by non-covalent forces and the inhibitor maintains a reversible equilibrium with the enzyme.
 - Reversible inhibitors can be competitive, noncompetitive, and uncompetitive inhibitors.

Competitive inhibition

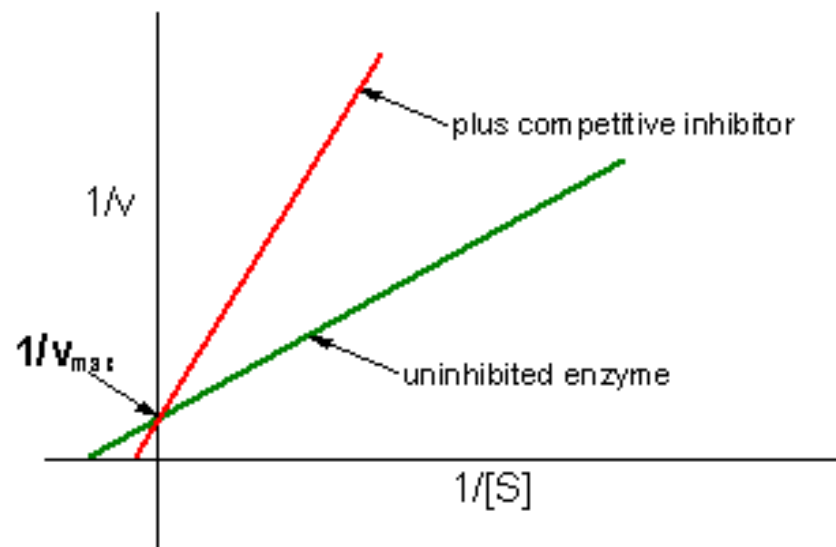
- In competitive inhibition, the inhibitor competes with the substrate for the active site.
- Because increasing the amount of substrate can overcome the inhibition, V_{max} can be reached in the presence of a competitive inhibitor.
- In the presence of a competitive inhibitor, an enzyme will have the same V_{max} as in the absence of an inhibitor, but the value of K_M is increased.



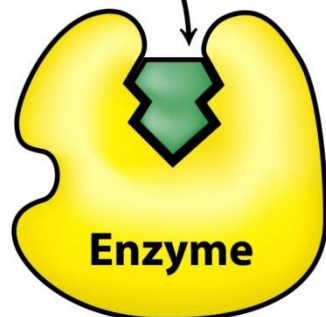
Panel A



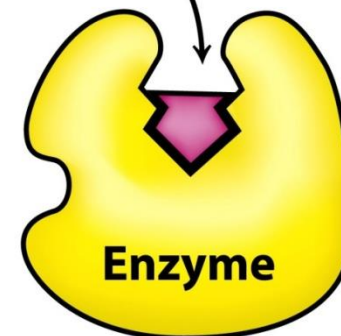
Panel B



Substrate

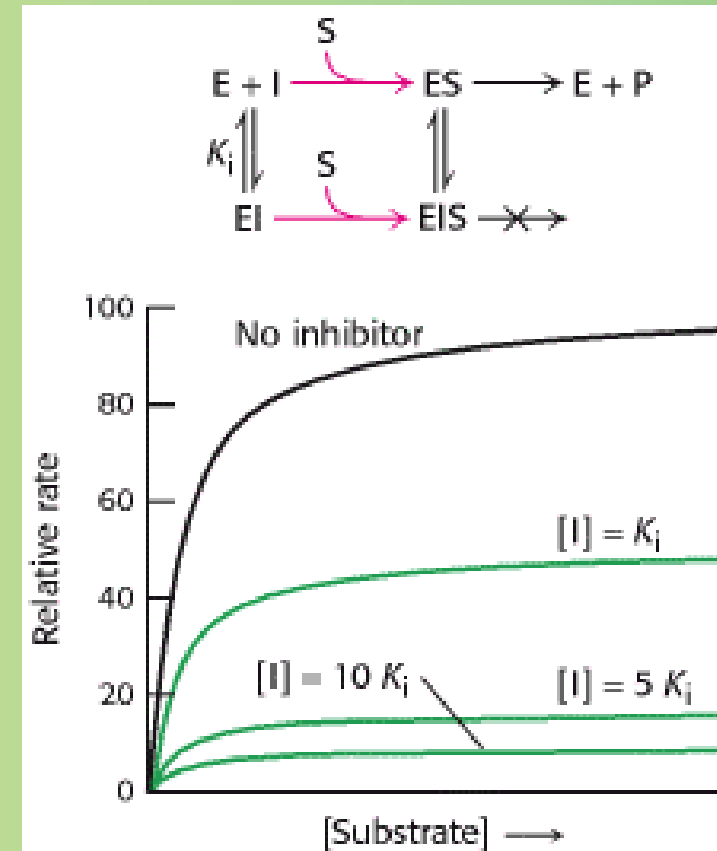


Competitive inhibitor

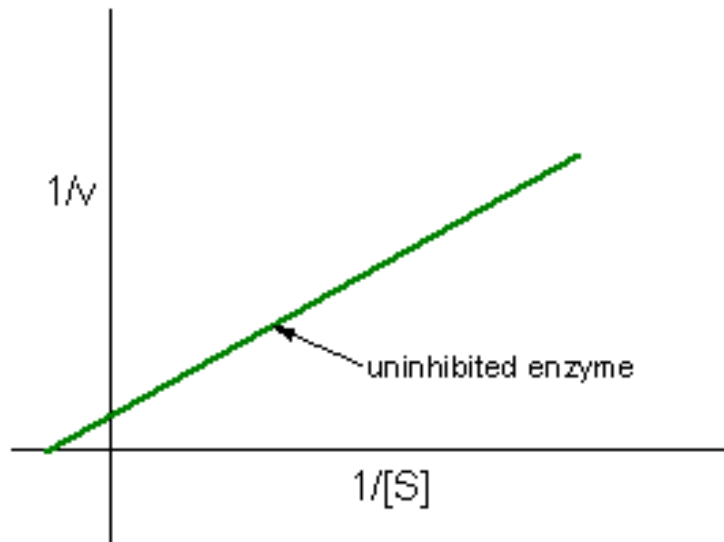


Noncompetitive inhibition

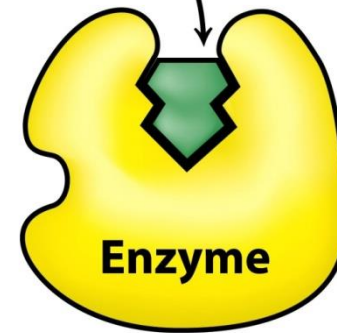
- In noncompetitive inhibition, the inhibitor binds E or ES complex at a site other than the catalytic site
- Substrate can also bind to the enzyme-inhibitor complex
- However, the enzyme-inhibitor-substrate complex does not proceed to form product
- The value of V_{max} is decreased while the value of K_M is unchanged
- Noncompetitive inhibition cannot be overcome by increasing the substrate concentration



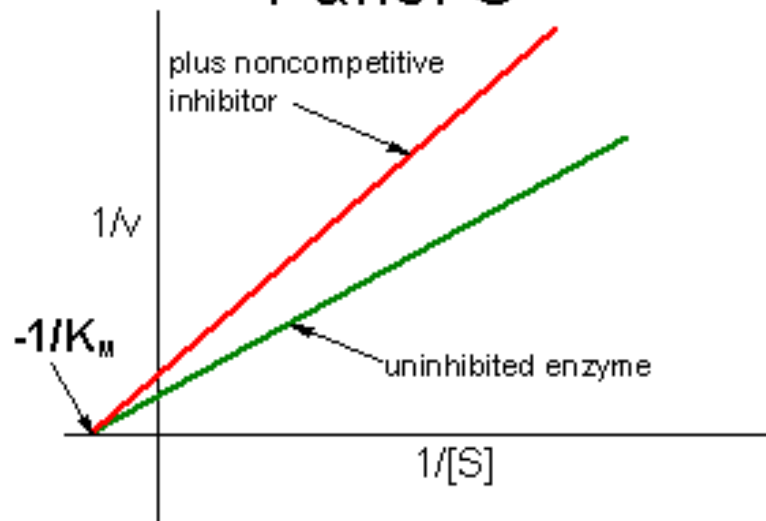
Panel A



Substrate



Panel C



Substrate

Noncompetitive inhibitor

